

Use of fractional factorial design for optimizing removal of nickel, copper, cadmium and lead by buriti modified fibers

D. Q. MELO¹, C. B. VIDAL², G. S.C. RAULINO³, J. T. OLIVEIRA¹, R. N. P. TEIXEIRA³ E R.F. NASCIMENTO¹

¹ Universidade Federal do Ceará, Departamento de Analítica e Físico-Química

^{2,3} Universidade Federal do Ceará, Departamento de Engenharia Hidráulica e Ambiental

E-mail para contato: diegodqm@gmail.com

RESUMO – The adsorption of copper, cadmium, lead and nickel in mono-element and multi-element aqueous solutions onto buriti modified fibers was studied. The fractional factorial design 2^{4-1} showed that pH, adsorbent mass, agitation rate and initial metal concentration influenced each metal adsorption differently. The kinetics and thermodynamic equilibrium parameters were obtained for all elements. The results showed that the order of mono-element adsorption for these three contaminants is Ni > Cd > Pb > Cu. The adsorption kinetics were fitted to the pseudo-second order model, giving linear correlation coefficients higher than 0.98. The Langmuir isotherm provided the best fit with the mono-element experimental data. In this study, the multi-element system isotherms were also obtained and a significant difference was found in the competitiveness for the site and the adsorption capacity order was Ni > Cu > Cd > Pb.

1. INTRODUCTION

Recently, a progressive increase in industrialization and urbanization has substantially enhanced the aquatic environmental pollution by the discharge of industrial effluents containing various pollutants. Among these, the toxic metals produced and consumed by various industrial sectors such as mining, textiles, painting, electroplating, refining and pesticides generate a huge volume of toxic wastewater contaminated with highly toxic metals. Some general techniques for heavy metals removal are ion exchange, nanofiltration, precipitation and activated carbon adsorption. Among the various techniques, adsorption from waste is very popular due to its low cost and simplicity (MELO, *et al.* 2013). Various lignocellulose-derived materials have been studied as adsorbents including cellulosic substrates, sugar cane bagasse (SOUSA *et al.* 2009), cashew bagasse (MOREIRA *et al.* 2009), coconut shell (NETO *et al.* 2012). A major advantage of using natural fibers as adsorbents is the ready availability of renewable sources in nature, the low costs, the biodegradability, as well as the excellent mechanical properties. The present work focuses on removal of Cd^{2+} , Cu^{2+} , Ni^{2+} and Pb^{2+} ions from aqueous multi-element solutions using buriti fibers as an adsorbent. The importance of working with multi-element solutions is the simulation of industrial effluents, since most contain two or more pollutants, as desiring a more effective and versatile adsorbent. However, it is important to highlight the effect of competition for the active sites of the adsorbent, which affects the adsorption capacity and can be altered with changing and / or other parameters studied.

2. MATERIALS AND METHODS

2.1 Materials

Analytical-grade chemicals and ultrapure water (Millipore Direct Q3 Water Purification System) were used to prepare the solutions. Multi-element stock solutions of Cd^{2+} , Cu^{2+} , Ni^{2+} , and Pb^{2+} ($500 \text{ mg}\cdot\text{L}^{-1}$) were prepared with $\text{Cd}(\text{NO}_3)_2\cdot 4\text{H}_2\text{O}$, $\text{Cu}(\text{NO}_3)_2\cdot 3\text{H}_2\text{O}$, $\text{Ni}(\text{NO}_3)_2\cdot 6\text{H}_2\text{O}$, and $\text{Pb}(\text{NO}_3)_2$ (Merck, São Paulo, Brazil), respectively. The acetate buffer was prepared with sodium acetate and glacial acetic acid. NaOH ($0.10 \text{ mol}\cdot\text{L}^{-1}$) and HCl ($0.10 \text{ mol}\cdot\text{L}^{-1}$) solutions were used for pH adjustments. Buriti fibers were supplied by Embrapa Tropical Agro-industry, CE, Brazil (EMBRAPA/CE).

2.2 Batch adsorption experiments

Batch adsorption experiments were conducted at room temperature (28°C) to study the effect of solution pH (4.5-5.5), initial ion concentration ($100\text{-}500 \text{ mg}\cdot\text{L}^{-1}$), agitation rate ($100\text{-}200 \text{ rpm}$) and the adsorbent mass ($0.05 - 0.150 \text{ g}$) until equilibrium was reached. The concentrations of Cu^{2+} , Cd^{2+} , Ni^{2+} and Pb^{2+} were measured with an atomic absorption spectrophotometer (933 plus, GBC, Australia). The equilibrium adsorption capacity of the adsorbent was calculated with eq 1

$$q_e = \frac{(C_o - C_e)V}{W} \quad (1)$$

where q_e is the equilibrium adsorption capacity q_e total equilibrium adsorption capacity (mg of metal/ g adsorbent), C_o is the initial concentration of the metal ion in $\text{mg}\cdot\text{L}^{-1}$, C_e is the equilibrium concentration of metal ion in $\text{mg}\cdot\text{L}^{-1}$, V is the volume of the solution in liters, and W is the mass of adsorbent in grams. All of the data presented are the mean values of two results obtained in identical essays. Variation coefficients were found to be lower than 5 %, and the statistical analysis was carried out with Microsoft Excel software.

2.3 Experimental Design and Statistical Analysis

A fractional factorial design was conducted to study the influence of four factors in the multi-element ion adsorption of Cu^{2+} , Pb^{2+} , Ni^{2+} and Cd^{2+} using buriti fibers as adsorbent (Table 1). Buriti fibers were added to multi-element solutions (25.0 mL) in 50 mL Erlenmeyer flasks. The mixtures were mechanically stirred for 2 h at $28 \pm 2^\circ\text{C}$.

Table 1 – Coded factors used in the 2^{4-1} fractional factorial design for studying the adsorption of Cu^{2+} , Pb^{2+} , Ni^{2+} and Cd^{2+} by buriti fibers

Code	Factor (unit)	(–)	0	(+)
A	pH	4.5	5.0	5.5
B	Adsorbent mass (mg)	50	100	150
C	Agitation rate (rpm)	100	150	200
D	Initial metal concentration ($\text{mg}\cdot\text{L}^{-1}$)	100	300	500

A two level fractional factorial design (2^{4-1}) with central point was applied to study the factors that most influence the response. The experiments were performed with four

replications in the corner points (combinations of ‘-’ and ‘+’ levels) and eight central points. The adsorption capacity, $q_{M(II)}$, of each metal and total adsorption capacity, q_{tot} , were the responses measured. The values of $q_{M(II)}$ were calculated using equation 1. The total adsorption capacity, q_{tot} , was calculated using the following relationship:

$$q_{tot} = \sum_{j=1}^4 \frac{(C_{0,j} - C_{e,j})}{W} V$$

where $C_{0,j}$ is the initial metal ion concentration (given in units of mg/L), $C_{e,j}$ the equilibrium metal ion concentration (also given in mg/L), W the adsorbent mass (given in units of g) and V the volume (given in units of L).

MINITAB statistical software (version 16) was used to design and analyze the fractional factorial experiments. The results were analyzed to estimate the effects of each factor on the adsorption process. Data were reported as mean \pm standard deviation at a significance level of $p < 0.05$. Pareto charts were constructed using the results of the Student’s t-test. The results obtained were fit to mathematical models using analysis of variance (ANOVA).

2.4 Adsorption kinetics

The multi-element solution was continuously shaken at pH appropriate. Aliquots of the supernatant were collected at regular time intervals, up to 60 min. Adsorption capacities were calculated by the differences between the initial and the final concentrations at any given time.

2.5 Adsorption isotherms

Bururi fibers were added to mono-element and multi-elements solutions in 50-mL Erlenmeyer flasks, with metal ion concentrations in the range of 20 mg.L⁻¹ to 500 mg.L⁻¹, at pH appropriate. The data obtained for the adsorption isotherms were described according to the Langmuir (Equation 2) and Freundlich (Equation 3) models:

$$q_e = \frac{q_{\max} K_L C_e}{(1 + K_L C_e)} \quad (2)$$

$$q_e = K_f C_e^{1/n} \quad (3)$$

where: C_e is the solute concentration at equilibrium (mg.L⁻¹), q_e is the amount of metal ion that is adsorbed at equilibrium (mg.g⁻¹), q_{\max} is the monolayer capacity of the adsorbent (mg.g⁻¹), and K_L is the Langmuir adsorption constant, which is related to the energy of adsorption (L.mg⁻¹). K_f (L.mg⁻¹) and n are Freundlich adsorption isotherm constants related to the saturation capacity and intensity of adsorption, respectively.

3. RESULTS AND DISCUSSION

3.1 Results of the Experimental Design and Statistical Analysis

The results obtained through the experimental design for multi-element metal ions adsorption using buriti fibers are presented at table 2. Based on the experimental data, the variables evidencing statistically significant effects were determined via t-test. The confidence degree was set at 95% ($\alpha = 0.05$) which means that variables having a confidence exceeding 95% ($P\text{-value} < 0.05$) were considered to have a significant effect on the responses.

Table 2 – Column assignment for the various factors in the fractional factorial design (2^{4-1}) and experimental values for multi-element metal ions adsorption

Run	Coded Factors				$q_{Cu(II)}$	$q_{Pb(II)}$	$q_{Ni(II)}$	$q_{Cd(II)}$	q_{tot}
	A	B	C	D*					
1	–	–	–	–	5.65 ± 1.23	16.15 ± 0.56	4.48 ± 0.84	8.74 ± 1.04	35.02 ± 2.72
2	+	–	–	+	26.93 ± 0.26	40.96 ± 0.84	22.14 ± 0.53	8.70 ± 0.76	98.72 ± 1.26
3	–	+	–	+	9.59 ± 0.87	18.99 ± 0.18	4.63 ± 0.51	6.01 ± 5.13	39.21 ± 5.69
4	+	+	–	–	8.77 ± 0.48	8.54 ± 0.72	2.19 ± 0.53	2.37 ± 0.44	21.88 ± 1.92
5	–	–	+	+	4.02 ± 0.68	32.94 ± 0.86	18.48 ± 0.91	21.22 ± 0.70	76.66 ± 1.83
6	+	–	+	–	9.60 ± 0.68	20.82 ± 0.85	4.76 ± 1.29	2.38 ± 1.61	37.55 ± 1.97
7	–	+	+	–	3.41 ± 0.67	7.50 ± 0.20	1.91 ± 0.28	1.34 ± 0.26	14.16 ± 1.17
8	+	+	+	+	20.41 ± 0.57	25.17 ± 0.38	13.53 ± 0.30	4.32 ± 0.91	63.43 ± 0.69
9	0	0	0	0	5.70 ± 0.30	8.50 ± 0.95	2.71 ± 0.82	4.34 ± 1.07	21.25 ± 1.86

* Generator: $I = ABCD$

The 2^{4-1} fractional factorial design is an example of experimental design of resolution IV. In this type of design it is possible to estimate main effects without confusion with two-factor interactions, but two-factor interaction effects are confounded with other two-factor interactions. This means that two-factor interaction effects are not precisely estimated. Instead we can estimate its contrasts. A contrast is a linear combination of two or more factor level means. The contrasts are formed according to the confounding pattern, also known as aliasing. The confounding pattern is determined by the defining relation (generator) of the model. The defining relation used in this work is $I = ABCD$. This notation is used in matricial equations and can be used to determine all the relations between factors. From the defining relation of the model one can easily see that main effects are free from aliasing with two-effect interaction effects, but are confounded with three-factor interaction effects ($A = BCD$; $B = ACD$; $C = ABD$; $D = ABC$). Thus the contrasts between the main effects and the three-factor effects are $I_A = A + BCD$; $I_B = B + ACD$; $I_C = C + ABD$; $I_D = D + ABC$. One can also prove that two-interaction effects follow the relations $AB = CD$; $AC = BD$; $AD = BC$. The contrasts of two-interaction effects are $I_{AB} = AB + CD$; $I_{AC} = AC + BD$; $I_{AD} = AD + BC$. According to Box, Hunter and Hunter (1978) the higher order interaction effects (3- and 4-factor interactions in this study) are often negligible and can be ignored. Thus, the main effects can be obtained without confusion with higher order interaction effects. The Pareto charts for $q_{Cu(II)}$, $q_{Pb(II)}$, $q_{Ni(II)}$, and $q_{Cd(II)}$ are presented in figure 1. Observing figure 1 it can be seen that all main

effects influence $q_{Cu(II)}$ and $q_{Ni(II)}$, and the only non-significant main effect for $q_{Pb(II)}$ and $q_{Cd(II)}$ is C (agitation rate).

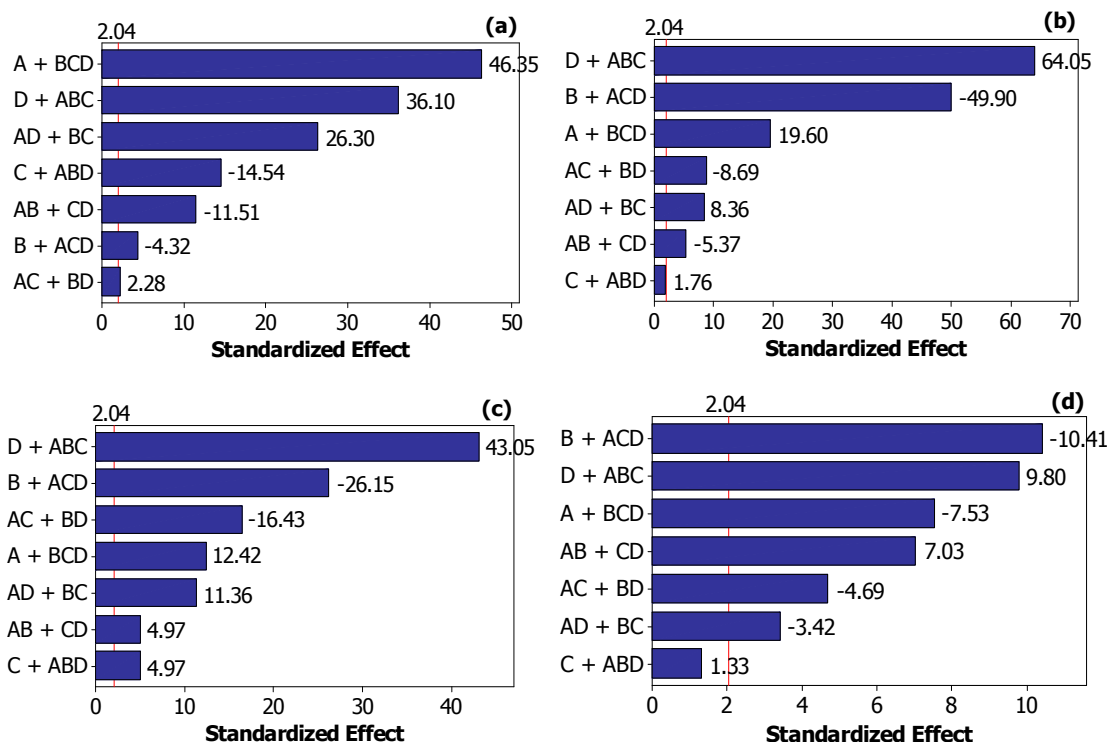


Figure 1 – Standardized Pareto charts showing main effects of experimental parameters on responses at the confidence limit of 95% for: (a) $q_{Cu(II)}$, (b) $q_{Pb(II)}$, (c) $q_{Ni(II)}$, and (d) $q_{Cd(II)}$.

It is important to remember that in a multi-element system the competition effect have to be taken into account when assessing the effect of each factor on the adsorption of each metal. The overall adsorption uptake is a good way to measure the efficiency of the adsorption process in multi-element solutions. The Pareto chart for q_{tot} is presented in figure 2. The main effects affecting the response are D (initial metal concentration), B (adsorbent mass) and A (pH). Variable C (agitation rate) is not statistically Significant in this interval studied. This suggests that the film around the particle is overcome in the investigated range (100 to 200 rpm) leading to similar responses.

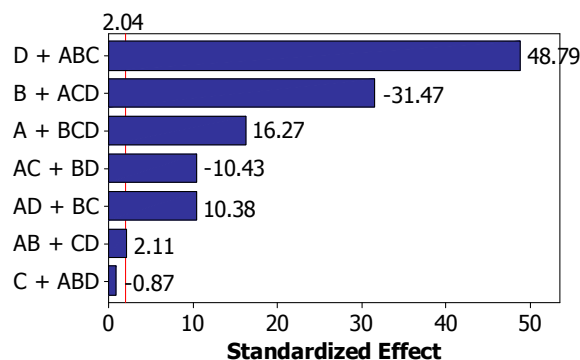


Figure 2 – Standardized Pareto charts showing main effects of experimental parameters on responses at the confidence limit of 95% for q_{tot} .

The analysis of variance (ANOVA) results for $q_{Cu(II)}$, $q_{Pb(II)}$, $q_{Ni(II)}$, and $q_{Cd(II)}$ are shown at table 3. The ANOVA results indicate the significance of the models ($P = 0.05$) showing that there are relationships between factors and responses. The determination coefficients at 95% of confidence level were 0.9921, 0.9958, 0.9892 and 0.8998, for $q_{Cu(II)}$, $q_{Pb(II)}$, $q_{Ni(II)}$, and $q_{Cd(II)}$, respectively.

Table 3 – Analysis of Variance (ANOVA) for each metal capacity adsorption

		$q_{Cu(II)}$				$q_{Pb(II)}$			
Source	DF	SS	MS	F	P	SS	MS	F	P
Model	8	2128.15	266.02	616.87	0.000	4750.35	593.79	1151.78	0.000
A	1	926.26	926.26	2147.91	0.000	197.95	197.95	383.97	0.000
B	1	8.04	8.04	18.64	0.000	1283.51	1283.51	2489.63	0.000
C	1	91.13	91.13	211.32	0.000	1.59	1.59	3.08	0.089
D	1	562.03	562.03	1303.30	0.000	2114.93	2114.93	4102.32	0.000
AB	1	57.10	57.10	132.42	0.000	14.89	14.89	28.88	0.000
AC	1	2.24	2.24	5.20	0.030	38.94	38.94	75.53	0.000
AD	1	298.28	298.98	691.69	0.000	36.01	36.01	69.86	0.000
Curvature	1	183.07	183.07	424.52	0.000	1062.53	1062.53	2060.98	0.000
Pure Error	31	13.37	0.43			15.98	0.52		
		$R^2 = 0.9938, R^2_{adj} = 0.9921$				$R^2 = 0.9966, R^2_{adj} = 0.9958$			

		$q_{Ni(II)}$				$q_{Cd(II)}$			
Source	DF	SS	MS	F	P	SS	MS	F	P
Model	8	2003.40	250.42	449.57	0.000	1205.28	150.66	44.76	0.000
A	1	85.95	85.95	154.29	0.000	190.87	190.87	56.70	0.000
B	1	380.81	380.81	683.64	0.000	364.48	364.48	108.28	0.000
C	1	13.73	13.73	24.65	0.000	5.92	5.92	1.76	0.194
D	1	1032.31	1032.31	1853.22	0.000	323.05	323.05	95.97	0.000
AB	1	13.75	13.75	24.69	0.000	166.32	166.32	49.41	0.000
AC	1	150.33	150.33	269.87	0.000	74.06	74.06	22.00	0.000
AD	1	71.87	71.87	129.01	0.000	39.29	39.29	11.67	0.002
Curvature	1	254.65	254.65	457.15	0.000	41.29	41.29	12.27	0.001
Pure Error	31	17.27	0.56			104.35	3.37		
		$R^2 = 0.9915, R^2_{adj} = 0.9892$				$R^2 = 0.9203, R^2_{adj} = 0.8998$			

The ANOVA results for q_{tot} are shown at table 4. The determination coefficient at 95% of confidence level was 0.9916, which demonstrates the high correlation between observed and predicted values while the rest (0.84%) was explained by the residues.

Table 4 – Analysis of Variance (ANOVA) for q_{tot}

Source	Sum of squares	DF	Mean square	F	P
Model	27949.0	8	3493.6	579.49	0.000
A	1596.8	1	1596.8	264.85	0.000
B	5970.2	1	5970.2	990.27	0.000

<i>C</i>	4.6	1	4.6	0.76	0.389
<i>D</i>	14351.7	1	14351.7	2380.52	0.000
<i>AB</i>	26.9	1	26.9	4.47	0.043
<i>AC</i>	655.9	1	655.9	108.79	0.000
<i>AD</i>	649.3	1	649.3	107.70	0.000
Curvature	4693.6	1	4693.6	778.53	0.000
Pure Error	186.9	31	6.0		

 $R^2 = 0.9934, R^2_{adj} = 0.9916$

Table 5 shows the regression equations for the five responses analyzed in the experimental design. The term *CtPt* in the equations is the curvature in the model introduced by the addition of a central point. It indicates that the relationship between the variables is not linear. The fitted equations can be used to estimate the results of an adsorption experiment. The maximum value for total adsorption, q_{tot} , according to the fitted model, is obtained maintaining factors *A* (pH) and *D* (initial metal concentration) at higher level (+1) and factors *B* (adsorbent mass) and *C* (agitation rate) at lower level (−1). Following that set of factors the model indicates a total adsorption of 98.34 mg g^{−1}. That set of conditions corresponds exactly to run number 2 in table 2, which resulted in an adsorption capacity of 98.72 ± 1.26 mg g^{−1}, a value in good accordance with the predicted result.

Table 5 – Regression Equations of the Fitted Models in Terms of Coded Values

$q_{Cu(II)} = 11.05 + 5.38*A - 0.50*B - 1.69*C + 4.19*D - 1.34*A*B + 0.27*A*C + 3.05*A*D - 5.35*CtPt$
$q_{Pb(II)} = 21.38 + 2.49*A - 6.33*B + 8.13*D - 0.68*A*B - 1.10*A*C + 1.06*A*D - 12.88*CtPt$
$q_{Ni(II)} = 9.02 + 1.64*A - 3.45*B + 0.66*C + 5.68*D + 0.66*A*B - 2.17*A*C + 1.50*A*D - 6.31*CtPt$
$q_{Cd(II)} = 6.88 - 2.44*A - 3.38*B + 3.18*D + 2.28*A*B - 1.52*A*C - 1.11*A*D - 2.54*CtPt$
$q_{tot} = 48.33 + 7.06*A - 13.66*B + 21.18*D + 0.92*A*B - 4.53*A*C + 4.50*A*D - 27.08*CtPt$

A = pH; *B* = adsorbent mass; *C* = agitation rate; *D* = initial metal concentration; *CtPt* = Central Point.

3.2 Adsorption kinetics

The equilibrium times found for the adsorption of metal ions onto Buriti fibers (15% NaOH) were: 15 min for Cu²⁺, Cd²⁺, and 5 min for Ni²⁺ and Pb²⁺. Pseudo-first order (PFO), pseudo second-order (PSO) and models were applied to monitor the kinetics of the adsorption process(es) and the prevailing mechanism(s). The experimental values for the adsorption capacities values (q_e) were found to be in agreement with those of the theoretical adsorption capacities (q_c) that were calculated by the PSO model as supported by the R^2 values and error functions(not shown). Results were also adjusted the diffusion models of weber Morris²² (not shown). However, the experimental data did not fit the model, indicating that the interaction between adsorbent and adsorbate occurs on the outer surface of the material.

3.4 Adsorption isotherms

Adsorption isotherms of the metal ions studied onto buriti fibers (15% NaOH) were obtained by plotting the concentration of each metal ion adsorbed on the solid phase (q) versus its concentration in the liquid phase (C_e) (MELO, *et al.* 2013). Evaluation of the experimental data by the theoretical models revealed that the Langmuir model adequately described the adsorption mechanism in a mono-element system for all metal ions studied. The adsorption capacities ($q_{\max}(\text{mg g}^{-1})$) followed the order: $\text{Ni}^{2+}(312.91) > \text{Cd}^{2+}(202.43) > \text{Pb}^{2+}(178.94) > \text{Cu}^{2+}(175.75)$. For a better comparison of the binding affinities, adsorption essays were also performed in the multi-element solutions containing the same amounts of each one of the metals studied. This, for the multi-element system the adsorption capacity order was $\text{Ni} > \text{Cu} > \text{Cd} > \text{Pb}$.

5. CONCLUSÕES

Experimental design results showed that the factors studied influenced each metal adsorption differently. The adsorption kinetics indicated that the multi-element adsorption equilibrium was reached within 15 min for all metal ions studied and that the experimental data best fitted to the pseudo-second order kinetic model. The analysis of the isotherms by the non-linear model showed that the experimental data for Cd^{2+} , Cu^{2+} , Ni^{2+} and Pb^{2+} were best described by the Langmuir model as high R^2 values. The maximum adsorption (mg g^{-1}) capacities followed the order: $\text{Ni}^{2+}(312.91) > \text{Cd}^{2+}(202.43) > \text{Pb}^{2+}(178.94) > \text{Cu}^{2+}(175.75)$.

6. REFERÊNCIAS

- BOX, G. E.; HUNTER, W. G.; HUNTER, J. S. *in Statistics for Experiments*, Wiley, New York, 1978.
- MELO, D. Q.; GOMES, E. C. C.; RAULINO, G. S. C.; LONGHINOTTI, E.; NASCIMENTO, R. F. Adsorption equilibria of Cu^{2+} , Zn^{2+} , and Cd^{2+} on EDTA-functionalized silica *J. Chem. Eng. Data* **2013**, 58; 798-806.
- MOREIRA, S. A.; SOUSA, F. W.; OLIVEIRA, A. G.; BRITO, E. S.; NASCIMENTO, R. F. Remoção de metais de solução aquosa usando bagaço de caju *Quim. Nova.* **2009**, 32, 1717-1722.
- NETO, V. O. S.; CARVALHO, T. V.; HONORATO, S. B.; GOMES, C. L.; FREITAS, F. C.; SILVA, M. A. A.; FREIRE, P. T. C.; NASCIMENTO, R. F. Coconut bagasse treated by thiourea/ammonia solution for cadmium removal: kinetics and adsorption equilibrium. *Bioresources* **2012**, 7, 1504-1524.
- SOUSA, F. W.; SILVA, M. J. B.; OLIVEIRA, I. R. N.; OLIVEIRA, A. G.; CAVALCANTE, R. M.; FECHINE, P. B. A.; SOUSA NETO, V. O.; DE KEUKELEIRE, D.; NASCIMENTO, R. F. Evaluation of a low-cost adsorbent for removal of toxic metal ions from wastewater of an electroplating factory *J. Environ. Manage.* **2009**, 89, 1-5.